

Name Key Hour \_\_\_\_\_**Practice TEST for Circular Motion/Gravity/Pendulums**

1. A pilot (72 kg) is flying a small plane in a circular path with a radius of 50 m. If it takes him 15.7 sec to make 1 circle, calculate the centripetal force acting on him.

$$\textcircled{1} v = \frac{2\pi r}{T} \quad \frac{2(\pi)(50)}{15.7} = 20 \frac{\text{m}}{\text{s}} \quad \textcircled{2} F_c = \frac{mv^2}{r} \quad \frac{72(20^2)}{50} = \boxed{576 \text{ N}}$$

2. Calculate the force of attraction between the Earth and the moon if the distance from center to center is  $3.84 \times 10^8 \text{ m}$ .

$$F_g = \frac{Gm_1 m_2}{r^2} = \frac{G(5.98 \times 10^{24} \text{ kg})(7.35 \times 10^{22} \text{ kg})}{(3.84 \times 10^8)^2} = \boxed{1.99 \times 10^{20} \text{ N}}$$

3. How far away from the center of the earth ( $r$ ) would you (100 kg) need to go in order for the acceleration due to gravity to be equal to  $2.9 \text{ m/s}^2$ ? What would your **weight** be there? How **many g's** would you feel?

$$\textcircled{1} g = \frac{GM}{r^2}$$

$$2.9 \frac{\text{m}}{\text{s}^2} = \frac{G(5.98 \times 10^{24})}{r^2}$$

$$\boxed{r = 1.17 \times 10^7 \text{ m}}$$

$$\textcircled{2} W = m \cdot g$$

$$(100)(2.9 \frac{\text{m}}{\text{s}^2})$$

$$= \boxed{290 \text{ N}}$$

$$\textcircled{3} g\text{'s} = \frac{290 \text{ N}}{100(9.8)}$$

$$= \boxed{0.296 g\text{'s}}$$

4. A satellite for AT&T is orbiting at 450,000 m above the surface of the earth. Calculate how fast it is traveling in **mph**.

$$r = 450,000 + 6.37 \times 10^6 = 6,820,000 \text{ m}$$

$$\textcircled{1} g = \frac{GM}{r^2} = \frac{G(5.98 \times 10^{24})}{6,820,000^2} = 8.575 \frac{\text{m}}{\text{s}^2}$$

$$\textcircled{2} g = \frac{v^2}{r} \quad 8.575 = \frac{v^2}{6,820,000}$$

$$v = 7648 \frac{\text{m}}{\text{s}} \times \frac{1 \text{ mi}}{1609 \text{ m}} \times \frac{3600 \text{ sec}}{1 \text{ hr}} = \boxed{17110 \text{ mph}}$$

5. What are the **definitions and units** for the following items: gravitational force, centripetal force, centrifugal force, mass, G, period

gravitational force ( $F_g$ ) - Force of attraction between 2 objects (N)  
 centripetal force ( $F_c$ ) - Force needed to keep an object moving in a circle (N)  
 centrifugal force - inertia  
 mass - amount of matter (kg)  
 G - universal gravitation constant ( $6.67 \times 10^{-11} \text{ N} \cdot \frac{\text{m}^2}{\text{kg}^2}$ )  
 period - time to make 1 revolution (sec)

6. How many meters long should a pendulum on earth be to have a period of 1.5 sec if the mass is 3.5 kg?

$$T^2 = \frac{4\pi^2 L}{g}$$

$$1.5^2 = \frac{4\pi^2 L}{9.8}$$

$$L = 0.559 \text{ m} \\ \text{or } 55.9 \text{ cm}$$

7. What affect does mass have on the period of a pendulum?

None!

8. What affect does length have on the period of a pendulum?

longer length = longer period

9. Find the period (T) of a pendulum with a length of 0.84 m on the International Space Station which is 344,000 m above the surface of the Earth.

$$r = 6.37 \times 10^6 + 344,000 = 6,714,000$$

$$\textcircled{1} g = \frac{Gm}{r^2} = \frac{6.67(5.98 \times 10^{24})}{(6,714,000)^2} = 8.85 \text{ m/s}^2$$

$$\textcircled{2} T^2 = \frac{4\pi^2 L}{g} = \frac{4\pi^2(0.84)}{8.85} \Rightarrow T^2 = 3.75$$

$$T = 1.94 \text{ sec}$$